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APR 77 W H HARPER, P N MARINOS

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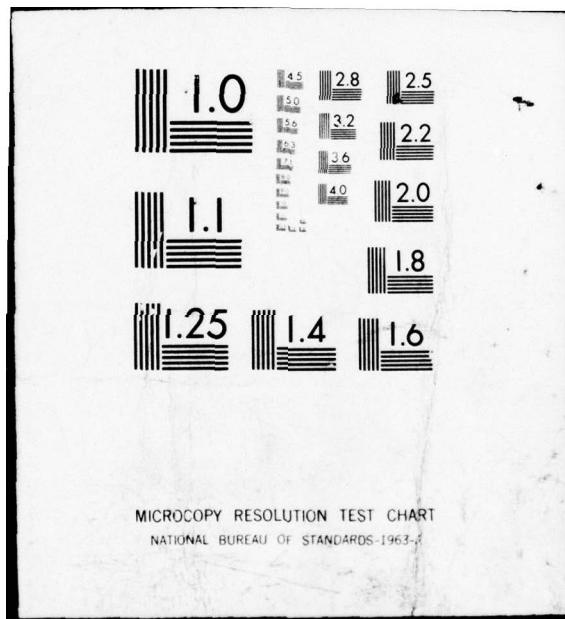
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NRL Memorandum Report 3475

A Method for Computing Vertical-Plane Coverage Diagrams for Frequency Agile Pulse Radar Systems

W. H. HARPER AND PETER N. MARINOS

*Search Radar Branch
Radar Division*

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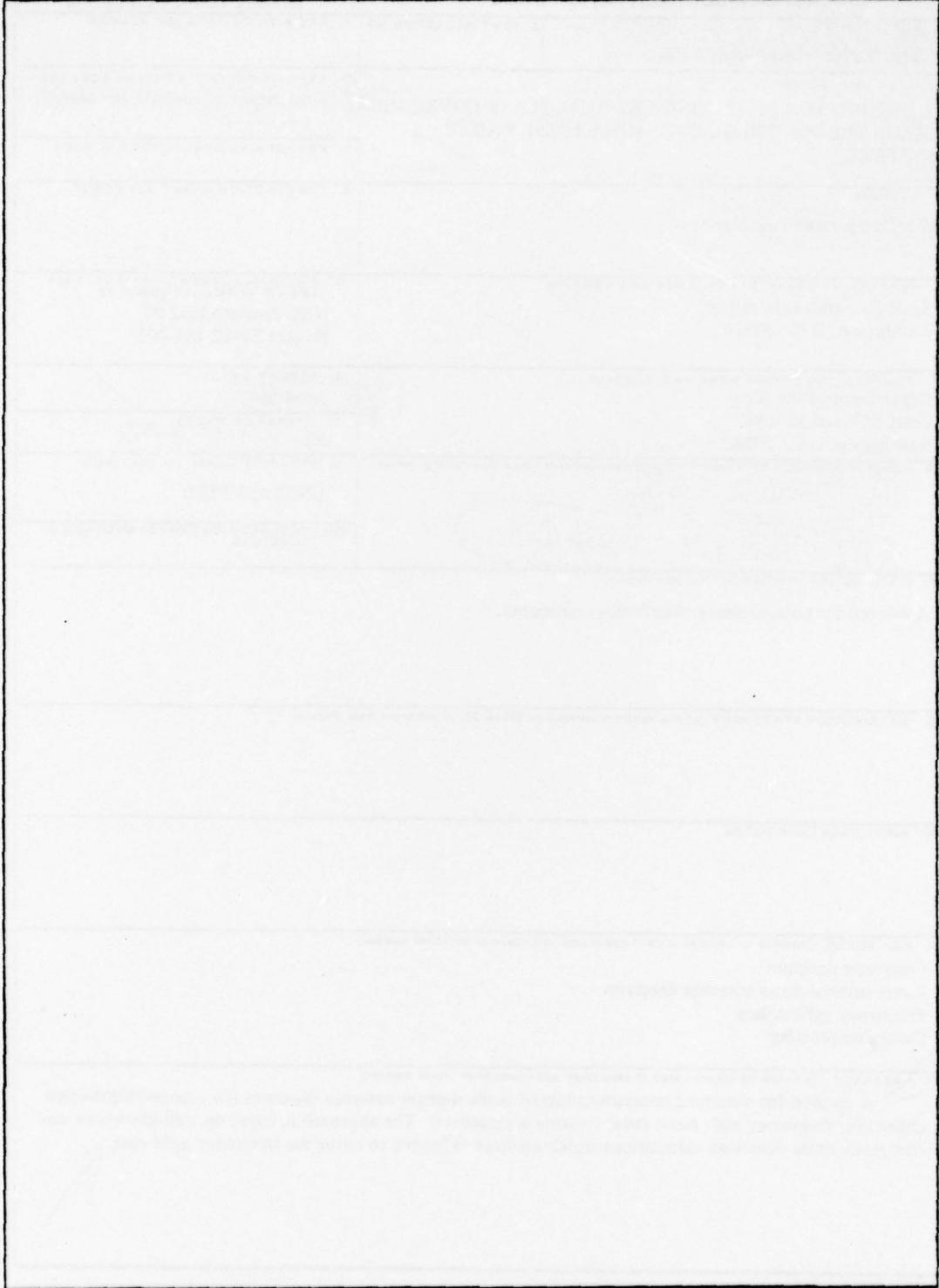
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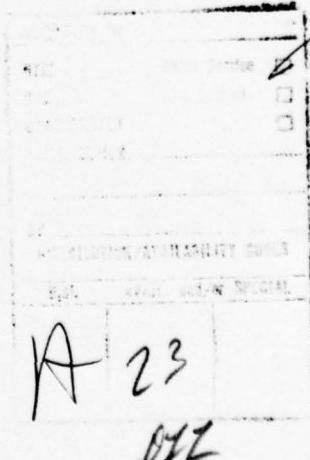
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A METHOD FOR COMPUTING VERTICAL-PLANE COVERAGE DIAGRAMS FOR FREQUENCY AGILE PULSE RADAR SYSTEMS

INTRODUCTION

In a comprehensive report on maximum radar range computations, Blake [1] provides all the necessary tools for obtaining coverage plots (i.e., range-height-angle charts) of monochromatic pulse radar systems. This paper provides a method for extending the range computations applicable to the monochromatic case to pulse radar systems featuring frequency agility. The number of different frequencies employed, as well as the number of consecutive pulses to be transmitted at the same frequency, are both arbitrary.

MATHEMATICAL ANALYSIS

The detection scheme assumed in the analysis which follows utilizes a square-law detector followed by a linear integrator, as shown in Fig. 1. The symbols D_o , X_o , and Y_o denote the SNR (i.e., signal-to-noise power ratio) at the designated points of the detector-integrator complex.

Based on approximate closed-form expressions derived by Barton [2] and later simplified by Cann [3], one may relate the input and output SNRs using the equation

$$X_o = \frac{2D_o^2}{D_o + 2.3} \quad (1)$$

The integrated output SNR, Y_o , may now be written in the form

$$Y_o = \sum_{j=1}^N X_{oj} = \sum_{j=1}^N \left\{ \frac{2D_{oj}^2}{D_{oj} + 2.3} \right\} \quad (2)$$

where N denotes the number of integrated pulses and D_{oj} represents the SNR at the detector input due to the j^{th} pulse illuminating a target located at R_{max} ; it is assumed that R_{max} represents the maximum detection range associated with the total energy delivered on the target by the N transmitted pulses.

Since our objective is to relate the integrated SNR (i.e., Y_o) to a maximum detection range, R_{max} , using the classical radar equation, an average SNR is defined at the detector output in the form

Note: Manuscript submitted March 4, 1977.

$$\hat{X}_o = \frac{1}{N} \sum_{j=1}^N X_{oj} \approx \frac{1}{N} \sum_{j=1}^N \frac{\frac{2D_{oj}^2}{D_{oj} + 2.3}}{(3)}$$

The SNR given by Eq. (3) may be thought of as the SNR necessary to achieve a specified probability of detection, P_d , and false alarm, P_{fa} , for a specified number of pulses and a postulated type of target; normally, it is the corresponding SNR, \hat{D}_o , at the input of the square-law detector rather than \hat{X}_o that one associates with P_d and P_{fa} . Given, however, \hat{D}_o , the corresponding value of \hat{X}_o is obtained using Eq. (1). For example, given N , P_d , and P_{fa} , and a target described by Swerling's Case 2, one may utilize published results [1] to determine \hat{D}_o and subsequently X_o .

Once \hat{X}_o is obtained, the problem becomes one of relating \hat{X}_o to a corresponding maximum detection range, R_{max} , in a way which takes advantage of the computational aids developed by Blake [1, 4]. This is accomplished by writing the radar equation in the form,

$$D_{oj} = \frac{P_t A^2 \sigma F_j^4}{4\pi \lambda_j^2 P_{noise} R_{max}^4} = \left[\frac{P_t A^2 \sigma}{4\pi \lambda_j^2 \hat{D}_o P_{noise}} \right] F_j^4 \cdot \frac{\hat{D}_o}{R_{max}^4} \quad (4)$$

where D_{oj} represents the SNR at the detector input due to the j^{th} pulse return from a target positioned at R_{max} ; \hat{D}_o is the (averaged) minimum SNR based on N pulses; F_j denotes the pattern-propagation factor; and the remaining symbols in Eq. (4) represent well-known radar parameters [5]. The bracketed portion of Eq. (4) represents the free-space range, R_{jfs}^4 , corresponding to N pulses, but as if they all had been transmitted at frequency f_j (i.e., wavelength λ_j) and each resulted in a SNR, \hat{D}_o , at the detector input. In view of the above interpretation, one may rewrite Eq. (4) in the form,

$$D_{oj} = \hat{D}_o \left(\frac{R_{xj}}{R_{max}} \right)^4 \quad (5)$$

where $R_{xj} = R_{jfs} F_j$, and $j = 1, 2, \dots, N$.

Since

$$R_{jfs}^4 = \frac{P_t A^2 \sigma}{4\pi \lambda_j^2 \hat{D}_o P_{noise}}, \quad (6)$$

varying only the frequency results in a relationship of the form

$$R_{jfs}^4 = R_{ifs}^4 \left(\frac{\lambda_i}{\lambda_j} \right)^2 = R_{ifs}^4 \left(\frac{f_j}{f_i} \right)^2 \quad (7)$$

which provides the free-space range at frequency f_j in terms of the free-space range at another frequency, f_i , while all other parameters in Eq. (6) remain fixed.

In some instances the maximum free-space range, $R_{j \max}$, based on the number of pulses at each frequency, is known. In this case, there is a \hat{D}_{oj} given by

$$\hat{D}_{oj} = \frac{P_t A^2 \sigma F_j^4}{4\pi \lambda_j^2 P_{noise} R_{j \max}^4} . \quad (8)$$

The free-space range at frequency f_j is then given by

$$R_{jfs}^4 = R_{j \max}^4 \left(\frac{\hat{D}_{oj}}{\hat{D}_o} \right) \quad (9)$$

Substituting next Eqs. (3) and (5) into Eq. (1), that is, into expression

$$\hat{X}_o = \frac{2\hat{D}_o}{1 + \alpha^2 \cdot 3 \left(\frac{1}{\hat{D}_o} \right)} \quad (10)$$

one obtains

$$\frac{1}{1 + \alpha} = \frac{1}{N} \sum_{j=1}^N \left[\frac{\left(\frac{R_{xj}}{R_{\max}} \right)^4}{1 + \alpha \left(\frac{R_{\max}}{R_{xj}} \right)^4} \right] \quad (11)$$

where $\alpha = (2.3/\hat{D}_o)$.

PLOTTING TECHNIQUES

Solution of Eq. (11) for R_{\max} provides the information necessary to produce the so-called radar vertical-plane coverage diagrams.

Blake [4] has developed a computer program for presenting the radar interference lobing phenomena on range-height-angle plots. This program was named LOBEPILOT and was written in Fortran for use on a CDC-3800 computer.

Relatively simple modifications to LOBEPILOT have been made which have resulted in the solution of Eq. (11) and enabled the computer (Calcomp) plotting of the lobing charts for frequency agile radars. The original modifications were made, and the program was debugged on a CDC-3800 computer at NRL. More

recently, the program has been changed to allow running on the new Texas Instruments Advanced Scientific Computer (ASC) at NRL. This new version has been named LOBMUF for "lobes, multi-frequency." The complete program is listed in Appendix A; the input data card formats are given in Appendix B.

In LOBMUF, P_d , P_{fa} , the total number of pulses integrated, the Swerling fluctuation case, and the number of radars or radar frequencies are specified on input data cards. In addition, for each radar or radar frequency, the free-space range, beamwidth, number of pulses at that frequency, sidelobe level, and a parameter FREF are required. FREF is zero if the free-space range was calculated at each frequency as indicated in connection with Eqs. (8) and (9); otherwise, FREF is the midband or average frequency and the free-space range corresponding to this reference frequency. Other inputs to the program are identical to those for LOBEPILOT. They concern the dimensions of the range-height chart, polarization radiated, antenna height and tilt, etc.

Using subroutines from another of Blake's computer programs [5], RGCALC, the signal-to-noise ratio, \hat{D}_0 , and the parameter, α , are computed. If FREF = 0, \hat{D}_{0j} for each frequency is calculated. Next, the pattern propagation factor, F_j , is calculated exactly as in Blake's LOBEPILOT. Finally, a simple search routine is used to converge on the value of R_{max} in Eq. (11). The search is terminated when the two sides of Eq. (11) differ by less than 0.01.

Figure 2 gives a typical coverage diagram generated by the computer program LOBMUF. The inputs involved a hypothetical radar radiating two pulses at each of 21 frequencies from 1350 MHz to 1650 MHz in 15 MHz steps. 1500 MHz was chosen as the reference frequency, and the free-space range was chosen to be 100 n. mi.

Figure 3 shows the lobing plot for a single frequency radar at 1500 MHz. A comparison of Figs. 2 and 3 shows that the incoherent integration in a frequency agile radar does much to fill in the nulls of the lobing pattern and give a solid elevation coverage.

SUMMARY

A computer program has been developed to plot range-height-angle lobing charts for frequency agile radars. This program is quite flexible. It may be used to plot the lobing charts for several radars or a single radar including several frequencies. This program, LOBMUF, builds on Blake's range-height charts and lobing plots. The program assumes incoherent integration and a closed form expression for a square-law detector.

ACKNOWLEDGMENT

Thanks are due to Dr. W. M. Waters of NRL for many helpful discussions concerning this problem.

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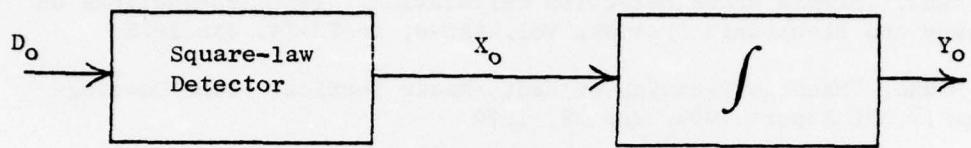
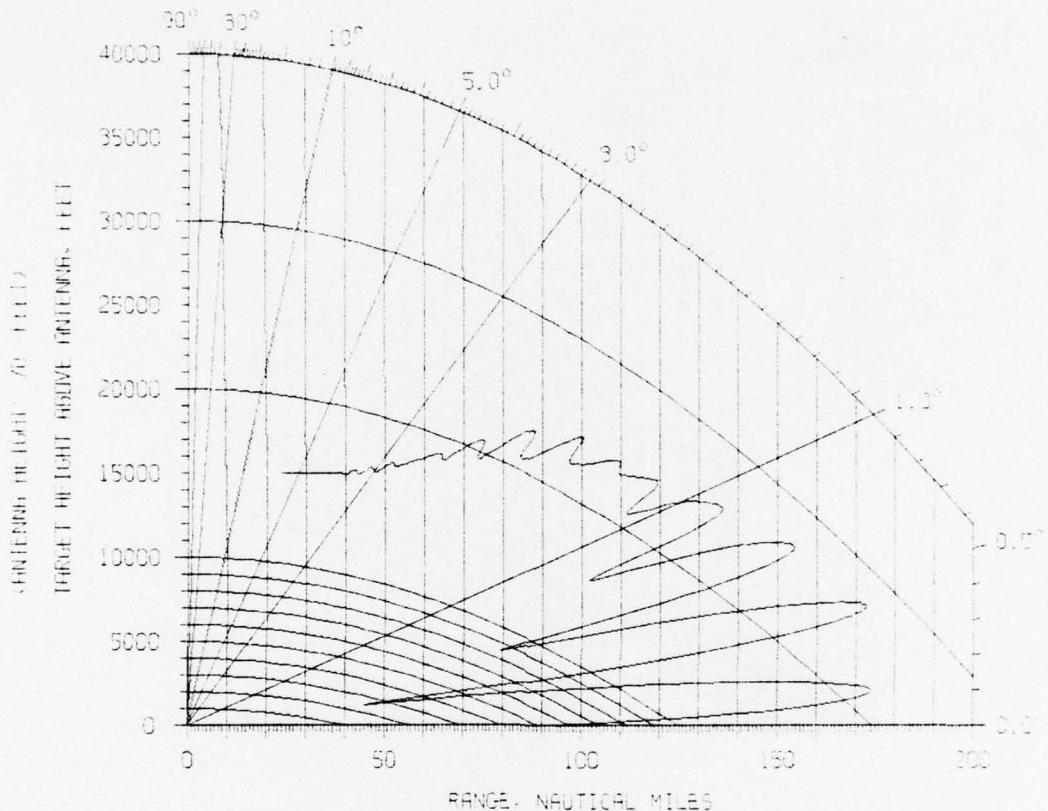


Fig. 1 — Radar detection and integration diagram

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R=1.65 TO 1.65 IN 0.015 STEPS, WH=4, RF=100, TILT=0, PD=-10, FULG=42

Fig. 2 — Lobing chart for hypothetical radar radiating two pulses at each of 21 frequencies from 1350 MHz to 1650 MHz in 15 MHz steps. Wave height of 4 feet, free-space range of 100 n. mi., and vertical beamwidth of 4.0° were assumed.

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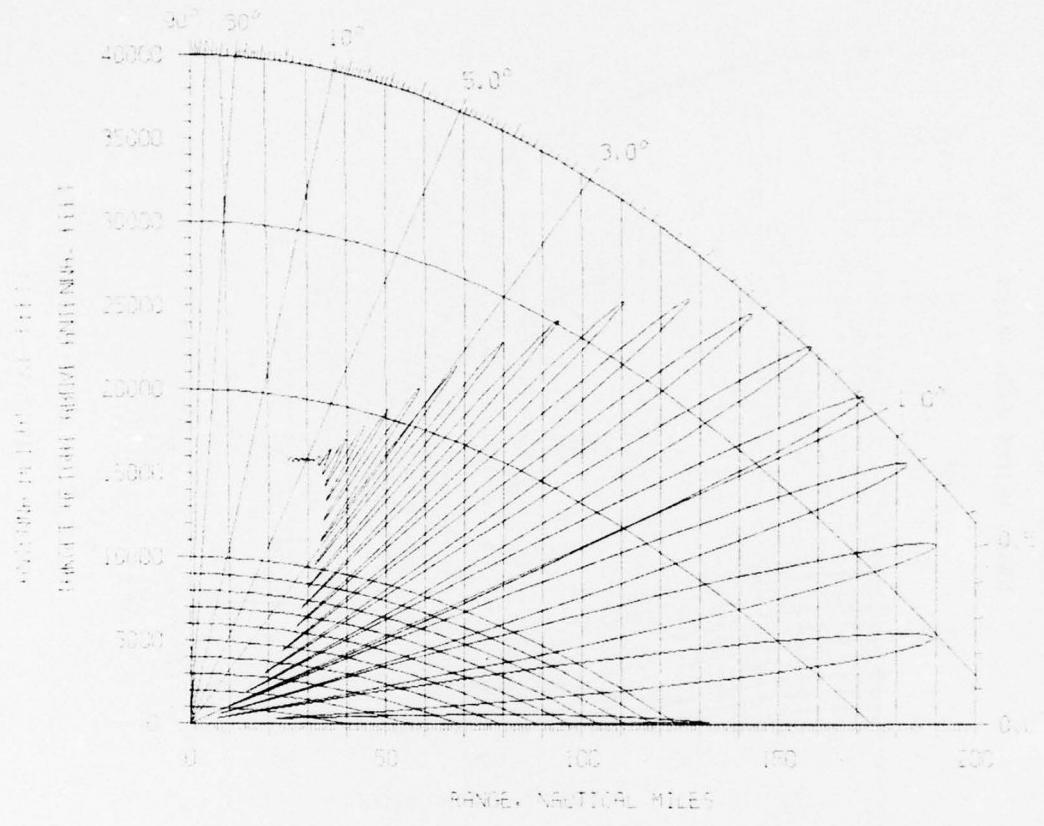


Fig. 3 — Lobing chart for single frequency radar at 1500 MHz with free-space range of 100 n. mi. A wave height of 4 feet and vertical beamwidth of 4.0° were assumed.

APPENDIX A: Fortran Listing for Program LOBMUF

The basic modifications to Blake's LOBEPILOT for program LOBMUF occur in Subroutine LOBES, as described in the Plotting Techniques section of this report. In addition, Subroutines PDSN, PD, INVERS, MARSWR, DGAM, DEVAL, GAM, EVAL, and SUMLOG are incorporated directly from RGCALC.

STATEMENT

```
PROGRAM L88MUF
REAL*8 ILABL(10)
COMMON /XTPR/ Q1,Q2,Q3,Q4,Q5,Q6,ERROR
COMMON/ADPLTS/IADD
COMMON/CSC/ICSC
COMMON/LT/LTN
DIMENSION A(1500)
DATA LTN/0/
CALL RSSTOP
READ 1,ANTHGT
ERROR=0.001
CALL PLOTS (A,1500,0.5)
PRINT 30
30 FORMAT (' TWO PEN TURRET POSITIONS ARE USED, D10 AND D11. PLOT ST
*ARTS WITH PEN TURRET POSITION D10. CHARGER PEN IS D11.'//)
2 READ (5,5,END=100) ILABL
200 READ 3,XMAX,YMAX,RMAX,HMAX,THMIN,THMAX,WHFT,RDR
NRDR=RDR
IF ( NRDR .LT. 1 ) GOTO 110
SFAC = YMAX*.125
52 H = .175*SFAC
Y = 1.5*SFAC
IF (LTN .EQ. 18) GO TO 61
IF ((YMAX+Y).LE.9.5) GO TO 61
60 SFAC = 9.5/(YMAX+Y)
YMAX = YMAX*SFAC
XMAX = XMAX*SFAC
Y = Y*SFAC
H = H*SFAC
61 X=Y+3.*H
CALL ORIGIN (X,Y)
PRINT 10, ILABL
CALL RHACHT (XMAX,YMAX,RMAX,HMAX,ANTHGT)
CALL L88ES (XMAX,YMAX,RMAX,HMAX,WHFT,THMIN,THMAX,NRDR)
CALL LETTER(0.,-Y,H,ILABL,0.0,B0)
CALL ORIGIN (XMAX+3.*Y,-Y)
CALL REZERO
GO TO 2
100 CALL ENOPLT
GOTO 130
110 PRINT 120,NRDR
120 FORMAT(//,' PROGRAM TERMINATION DUE TO ILLEGAL DATA ENTERED FOR NU
*MBER OF RADAPS . . . . NUMBER ENTERED IS ',I5)
130 CONTINUE
1 FORMAT (F10.0)
3 FORMAT( AF10.0)
5 FORMAT (10AB)
10 FRRMAT(3X,10AB//)
END
```

STATEMENT

```
C SUBROUTINE LOBES (XMAX,YMAX,RMAX,HMAX,WHFT,THMIN,THMAX,NRDR)
C THIS VERSION COMPLETED JUNE 1976 TO ALLOW PLOTTING LOBBING PATTERN
C FOR MULTIFREQUENCY CASE WITH INCOHERENT INTEGRATION.
COMMON/CSC/TCSC
COMMON /MTPE/ X2, Y2, X11, Y11, XA, YA, ERROR
COMMON/B/XX(181),YY(181),CT1(181),SN1(181),DELL
COMMON/DUM1/PFF( 2000 )
DIMENSION RXN4(50),NUM(50),SNP(50)
DIMENSION RFS(50),FMHZ(50),BD(50),SLDB(50)
DATA IIMAX/2000/
DATA ICSC / 0 /
DATA PI/3.141592654/
DATA PI2/6.283185307/
DATA RDN/.01745329252/
DATA CRNV/1.645788333E-4/
DATA AE / 2.786526684E7/
NRDS=NRDR
RNDS=FL9AT(NRDS)
READ 904,PDT,PFA,PULS,CASE,AHFT,TILT,PSL,CSC
PRINT 905,PDT,PFA,PULS,CASE,AHFT,TILT,PSL,CSC
905 FORMAT (/,2X,4HPDT=,F5.2,2X,4HPFA=,F5.2,2X,5HPULS=,F6.1,2X,5HCASE=
*,F5.2,2X,5HAHFT=,F6.1,2X,5HTILT=,F5.2,2X,4HPSL=,F4.1,2X,4HCSC=,F4.
*1,/)

NPULS=PULS
KASE=CASE
CALL PDSN (PDT,PFA,NPULS,KASE,SDR)
SNN=10.**(SDR/10.)
GAMMA=2.3/SNN
BETA=1./(1.+GAMMA)
904 FORMAT (8F10.0)
PRINT 590
590 FORMAT(' THE CALLING PARAMETERS SENT TO SUBROUTINE LOBES ARE AS FOL-
*LLOWS')
PRINT 591 , XMAX , YMAX , RMAX , HMAX , WHFT , THMIN , THMAX , NRDR
591 FORMAT(2X,5HXMAX=,F4.1,2X,5HYMAX=,F4.1,2X,5HRMAX=,F6.1,2X,5HHMAX=,
* F9.1,2X,5WHFT=,F5.1,2X,6HTHMIN=,F4.1,2X,6HTHMAX=,F4.1,2X,5HNRDR=
*,I3)
DO 84 II=1,IIMAX
84 PFF(II) = 0.0
E = YMAX*RMAX/(XMAX*HMAX*CRNV)
EX=XMAX/RMAX
Z=WHFT*.3535534
XP=1,E=45
YP=1,E=45
DO 801 JJ=1,NRDS
READ (5,802,END=807) RANGE,FREQ,BEAM,SLDB,PULNUM,FREQ
803 ICSC=CSC
IPOL=POL
NUM(JJ)=PULNUM
RFS(JJ)=RANGE
FMHZ(JJ)=FREQ
```

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STATEMENT

```
BWD(JJ)=BFEAM
SLDB(JJ)=SCLFB
802 FORMAT (6F10.0)
PRINT 499 , NRDR
499 FORMAT(//,20X,'THE RADAR PARAMETERS INPUT FOR RADAR NUMBER 1,13
*,,' ARE AS FOLLOWS')
PRINT 592,RFS(JJ),AHFT,FMHZ(JJ),BWD(JJ),SLDB(JJ),TILT,POL,CSC,PULN
*TUM,REF
592 FORMAT(//,2X,4HREFS=,F6.1,2X,5HAHFT=,F6.1,2X,5HFMHZ=,F7.1,2X,4HBWD=,
*F5.1,2X,5HSLDB=,F5.1,2X,5HTILT=,F5.1,2X,4HPOL=,F2.0,2X,4HCSC=,F2.0
*,2X,6HNPULS=,F5.0,2X,5HFREF=,F7.1/)
IF (FREF.NE.0.) GO TO 514
CALL PDSN (PCT,PFA,NUM(JJ),KASE,SDR)
SNR(JJ)=10.**(SDR/10.)
GO TO 515
514 SNR(JJ)=SNN
RFS(JJ)=RFS(JJ)*SQRT(SQRT(FMHZ(JJ)/FREF))
515 CONTINUE
RFS(JJ)=RFS(JJ)*(SQRT(SQRT(SNR(JJ)/SNN)))
NRDR=NRDR+1
801 CONTINUE
TILTR = TILT + RDN
THMINR=THMIN*FDN
THMAXR=THMAX*FDN
DEL1= ( THMAXR - THMINR ) / IIMAX
PI23DE = 3.0*DEL1 + PI2
THET2=THMINR-DEL1
N = 0
INDEX = 0
F=1.5
IDASH#1
CALL DASHON
AH2=AHFT*AHFT
AHE = 2. * AHFT/(3.*AE)
AEH = AE * (AE + AHFT)
PARAM = SQRT (AE/(2.*AHFT))
DO 810 II= 1,IIMAX
PF4=0.
THET2 = THET2 + DEL1
IF (THET2 .GE. PI23DE ) GOTO 40
T2 = TAN (THET2)
S2 = SIN(THET2)
S3 = S2
PSI = THET2
DO 805 M=1,NRDS
BWR=BWD(M)*FDN
BW2 = BWR*.5
CSCT = .7071 * SIN(BW2+TILTR)
IF (BWD(M).LE.45.) GO TO 251
250 IREAM=0
CONST=90./BWD(M)
```

STATEMENT

```

IF (BWD(M),EQ.360.) IBEM=1
GO TO 252
251 IBEM=1
CONST=1.39157/SIN(BW2)
ANLL=SARSIN(PI/CONST)
CPAT1=10.*((13.2-SLDB(M))*0.05)
252 W = 983.573/FMHZ(M)
W4 = 0.25 * *
WLIM = 0.01 * *
FAC = PI2/W
PD = 2. * AHFT * S2
IF (INDEX,EQ. 1) GO TO 77
T23 = T2/3.
GAM = HAE/(SQRT (T23**2+HAE)+T23)
PSI = THET2 + GAM
S3 = SIN(PSI)
ZETA = PARAM * T2
D1=0.57735*SQRT(1.+2.*ZETA/SQRT(ZETA*ZETA+3))
PD1=SQRT(AH2+AEH*GAM*GAM)*2.*S3*S3
IF (ABS(PD-PD1),GE.,WLIM) GO TO 79
78 IF (D1,LT.0.999) GO TO 79
780 D1 = 1.
INDEX = 1
79 PD = PD1
IF (PD,LT.,W4,BP,THET2,LT.0.000873) GO TO 300
GO TO 301
301 IF (IDASH,NE.1) GO TO 300
302 CALL CASHOF
IDASH=0
300 CONTINUE
77 CALL SEARFF (FMHZ(M),PSI,IPRL,RHO,PHI)
PIZ=PI+Z*S3/*
PIZ2=PIZ*PIZ
RUF=EXP(-B.*PIZ2)
ANG = THET2 - TILTR
IF(IBEM) 260,261,262
260 PAT=1.
GO TO 24
261 PAT=COS(CONST+ANG)
GO TO 24
262 IF (ICSC,NE.1) GO TO 61
80 IF (ANG,LE.,BW2) GO TO 61
60 PAT = CSCT/S2
GO TO 24
61 IF (ANG,NE.0.) GO TO 23
22 PAT = 1.
GO TO 24
23 UU = CONST * SIN (ANG)
INT = UU/PI2
DIFF = UU - INT * PI2
IF (ABS(ANG),LE.,ANLL) GO TO 161

```

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STATEMENT

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160 CPAT = CPAT1
      GO TO 162
161 CPAT = 1.
162 PAT = CPAT*SIN(DIFF)/UU
24 ANGR = THET2 + TILTR + 2. * GAM
      IF (IBEAM) 270,271,272
270 PATRS1.
      GO TO 27
271 PATR=CONS(CONST+ANGR)
      GO TO 27
272 IF (ANGR,NE.0.) GO TO 26
25 PATR = 1.
      GO TO 27
26 UUR = CONST * SIN(ANGR)
      INTR = UUR / PI2
      DIFFR = UUR - INTR * PI2
      IF (ABS(ANGR),LE.,ANLL) GO TO 66
65 CPAT = CPAT1
      GO TO 67
66 CPAT = 1.
67 PATR = CPAT*SIN(DIFFR)/UUR
27 IF (ABS(PAT),GE.1.E-44) GO TO 29
28 IF (PAT,GE.0.) GO TO 281
280 D = -RHO*RUF*PATR*1.E45*D1
      GO TO 30
281 D=D1*RHO*RUF*PATR*1.E45
      GO TO 30
29 D = D1* RHF * PATR/PAT * RUF
30 ALPHA = FAC * PD + PHI
      INT1 = ALPHA/PI2
      DIFF1 = ALPHA- INT1*PI2
      F = ABS(PAT)* SQRT(1.0 + D*D + 2.0*D*COS(DIFF1))
      RXN4(M)=(RFS(M)*F)**4
      PF4=PF4+SQRT(SQRT(RXN4(M)))/RNB
805 CONTINUE
      RNG=PF4
      RNG2=RNG*RNG
      RNG4=RNG2*RNG2
      FACMIN=10.
997 SUMEN=0.
      DO 998 MM=1,NRDS
      RRATIO=RXN4(MM)/RNG4
      PNS=FLGAT(NUM(MM))
      SUMEN=(PNS/PULS)*(RRATIO/(1.+GAMMA/RRATIO))+SUMEN
998 CONTINUE
      FACMN2=FACMIN
      FACMIN=SUMEN-BETA
      FSUM=FACTMN2+FACMIN
      IF (RNG,EQ.0.) GO TO 993
      IF (ABS (FACMIN),LT.0.01) GO TO 993
      IF (FACMIN,GE. -1.) GO TO 902

```

STATEMENT

```

901 HNUM=HINT(FACMIN)
FACMIN=FACMIN-HNUM
902 CONTINUE
RPREVRNG
RNG4=RNG4*(1.+FACMIN)
RNG=SGRT(SGRT(RNG4))
PDIFFSARS (RPREVRNG)
IF (PDIFF.LT.0.1.AND.FSLM.LT.0.01) GO TO 993
GO TO 997
993 CONTINUE
999 PFF(II)=RNG
910 CONTINUE
THET2=THMINR-DELI
DO 806 TI=1,IIMAX
A=PFF(II)*EX
THET2 = THET2 + DELI
N=N+1
X = A + COS(THET2)
Y = A + E * SIN(THET2)
45 IF (X.LE.XMAX) GO TO 501
500 ISUMX=0
GO TO 502
501 ISUMX=0
502 IF (Y.LE.YMAX) GO TO 504
503 ISUMY=0
GO TO 505
504 ISUMY=0
505 IF (XP.LE.XMAX) GO TO 507
506 ISUMXP=0
GO TO 508
507 ISUMXP=0
508 IF (YP.LE.YMAX) GO TO 510
509 ISUMYP=1
GO TO 511
510 ISUMYP=0
511 ISUM=ISUMX+ISUMY+ISUMXP+ISUMYP+1
GO TO (601,602,603,602,605,620,620,620,620,620,605,620),
*ISUM
601 IF (N,NE,1) GO TO 3
2 CALL PLST (X,Y,3)
X2=X
Y2=Y
XP=X
YP=Y
GOTO 806
3 IF (N,NE,2) GO TO 440
44 X=X
Y=Y
XP=X
YP=Y
X11=X

```

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STATEMENT

```
Y11=EY
GOTO 806
440 CALL MINTAP (X,Y)
620 X=P=X
Y=P=Y
IF (THET2.GE.THMAXR) G9 TO 40
GOTO 806
602 IF (N.EQ.1) G9 TO 620
CALL DASHON
IDASH=0
IF (IAxis.EQ.1) CALL PLST(XMAX,YMAX,2)
CALL INTRST (0., YMAX,XMAX,YMAX,X,Y,YP,YP,X0,Y0)
621 CALL PLST(X0,Y0,2)
CALL DASHOF
X2=X0
Y2=Y0
XA=X
X11=X
XP=X
YA=Y
Y11=EY
YP=Y
N=2
GOTO 806
603 IF (N.EQ.1) G9 TO 620
CALL DASHON
IDASH=0
CALL INTRST (XMAX,0.,XMAX,YMAX,X,Y,XP,YP,X0,Y0)
G9 TO 621
605 IF (N.EQ.1) G9 TO 620
CALL MINTAP (XP,YP)
CALL PLST(XP,YP,2)
CALL INTRST (0.,YMAX,XMAX,YMAX,X,Y,XP,YP,X0,Y0)
IAxis=2
CALL PLST(X0,Y0,2)
G9 TO 620
609 IF (N.EQ.1) G9 TO 620
CALL MINTAP (XP,YP)
CALL PLST(XP,YP,2)
CALL INTRST (XMAX,0.,XMAX,YMAX,X,Y,XP,YP,X0,Y0)
IAxis=1
CALL PLST(X0,Y0,2)
G9 TO 620
40 IF (ISUM.NE.1) G9 TO 651
650 CALL PLST(X,Y,2)
RETURN
651 IF (X.GT.XMAX.AND.XP.GT.XMAX) G9 TO 652
G9 TO 653
652 CALL INTRST (XMAX,0.,XMAX,YMAX,0.,0.,X,Y,X0,Y0)
CALL DASHON
IF (Y0.LE.YMAX) G9 TO 655
```

BEST AVAILABLE COPY

STATEMENT

```
654 CALL PLAT(XMAX,YMAX,2)
      CALL INTRST(0.,YMAX,XMAX,YMAX,0.,0.,X,Y,X0,Y0)
655 CALL PLAT(Y0,Y0,2)
      CALL DASHRF
      RETURN
653 IF (Y.GT.YMAX.AND.YP.GT.YMAX) GO TO 656
      GO TO 657
656 CALL DASHAN
      CALL INTRST(0.,YMAX,XMAX,YMAX,0.,0.,X,Y,X0,Y0)
      IF (X0.LE.XMAX) GO TO 659
658 CALL INTRST(XMAX,0.,XMAX,YMAX,0.,0.,X,Y,X0,Y0)
659 CALL PLAT(X0,Y0,2)
      CALL DASHOF
      RETURN
659 IF(IAXIS.EQ.1) CALL PLAT(XMAX,YMAX,2)
      GO TO 660
806 CONTINUE
807 GOTO 809
808 FORMAT(1H1,' END OF FILE HAS BEEN READ WHERE DATA CARD SHOULD BE')
809 END
```

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STATEMENT

```
SUBROUTINE POSN(PDT,PFA,NPULS,KASE,SDB)
EXTERNAL PD
DIMENSION DB0(5),SLOPE(5),PDFAC(5)
COMMON /PDS/ PFLAST,NLAST,KSLAST
DATA PFLAST/0./
DATA NLAST/0/
DATA KSLAST/-1/
DATA DB0/12.5,14.,14.,13.2,13.2/
DATA SLOPE/6.,7.,8.,7.,8./
DATA PDFAC/4.8,20.,20.,15.,13./
DATA DMIN/-30./
DATA DRMAX/50./
DATA DR1/0./
DATA DR2/0./
DATA PDLAST/0./
IF (PDT,NE.,PDLAST) GO TO 20
1 IF (PFA,NE.,PFLAST) GO TO 20
2 IF (NPULS,NE.,NLAST) GO TO 20
3 IF (KASE,EG.,KSLAST) RETURN
20 PDLAST=PDT
PFLAST=PFA
NLAST=NPULS
KSLAST=KASE
K=KASE + 1
PULS=NPULS
DR1=DB0(K)-SLOPE(K)*ALOG10(PULS)+(PDT=.5)*PDFAC(K)+(PFA=8.)*.4+1.
DR2=DR1+2.
CALL INVERS(DRMIN,DRMAX,DR1,DR2,4,15,NCI,SCR,PD1,PDT,PC)
END
```

STATEMENT

```
FUNCTION PD(SNDR)
COMMON/PDS/FAN,KASE
OPEN
FANSFA
KAS=KASE
CALL MARSAR (SNDR,NP,FAN,KAS,PD1)
PD=PD1
END
```

BEST AVAILABLE COPY

STATEMENT

```

SUBROUTINE INVERS(XMIN,XMAX,XLP,XHI,NSIG,LIM,NPI,X,F1,FT,F)
TEST = 10.**(-NSIG)
FD = FT
IF (FT .EQ. 0.) FD = 1.
NPI = 1
DELTA = XHI - XLP
X1=XLP
X2=XHI
F1=F(X1)
F2=F(X2)
SLOPE=(F2-F1)/(X2-X1)
IF (SLOPE.NE.0.) GO TO 21
10 FMAXSF(XMAX)
FMINSF(XMIN)
SLOPE = (FMAX-FMIN)/(XMAX-XMIN)
21 IF ((F2-FT)*SLOPE.GE.0.) GO TO 23
22 X1=X2
F1=F2
X2=X2+DELTA
IF (X2 .GT. XMAX) Y2=XMAX
F2=F(X2)
GO TO 21
23 IF ((FT-F1)*SLOPE.GE.0.) GO TO 25
24 X2=X1
X1=X1-DELTA
IF (X1 .LT. XMIN) X1=XMIN
F2=F1
F1=F(X1)
GO TO 23
25 XA=X1
XB=X2
FB=F2
IF (ABS(F2-FT).GE.ABS(F1-FT)) GO TO 6
7 F22=F2
F2=F1
F1=F22
X22=X2
X2=X1
X1=X22
GO TO 6
1 F1=F(X)
X1=X
TEST1 = ABS((F1-FT)/FD)
IF (TEST1.GT.TEST) GO TO 6
2 RETURN
6 IF(NPI.LT.LIM) GO TO 13
12 PRINT 40
PRINT 41, LIM
PRINT 42, XMIN, XMAX, XLP, XHI, NSIG, LIM, NPI, X, F1, FT
RETURN
13 IF (F1.NE.F2) GO TO 16

```

STATEMENT

```
15 IF (F1.NE.F2) GO TO 12
17 X5=X1
X2=X8
GO TO 19
18 X4=X1
X2=X4
19 X=(XA+XB)*.5
GO TO 1
20 X=(X1+X2)*(FT-F2)/(F1-F2) + X2
IF (X .LT. XA) X=X4
IF (X .GT. XB) X=XB
N3I = N3I + 1
F2=F1
X2=X1
GO TO 1
40 FORMAT (//'* MESSAGE FROM SUBROUTINE INVERS -- //')
41 FORMAT ('* FUNCTION INVERSION NOT ACCOMPLISHED WITHIN SPECIFIED '
*,I3,' ITERATIONS.')
42 FORMAT ('* INVERS PARAMETERS WERE ',4(E10.3,2X),3(I3,2X),E10.3,
* 2(2X,E10.3) //')
END
```

STATEMENT

```

SUBROUTINE MAPSWR (SNDR,N,FA,KASE,PN)
DOUBLE PRECISION ENPR,YBPR,GAMPR,PYB,H,Y0,E0,Y1,E1,STEP,YB
DOUBLE PRECISION DGAM, DEVAL, SUMLG, SUML, FAN, EN
SNR = 10.**(SNDR*.1)
MODE=1
IF (MODE) 800, 800, 900
900 FAN=DLG10(DLG(6,500)/DLG(1,-(10,00)**(-FA)))
GO TO 905
800 FAN = FA
905 IF(N) 99,99,2
2 IF(FA)99,99,3
3 IF(KASE) 99,4,4
4 IF(KASE=4) 5,5,99
5 ENPR = 0.
6 ENPR = FAN
EN = N
YBPR = 0.
IF (NPREV .EQ. N .AND. FAPREV .EQ. FA) GO TO 777
IF(N=12) 7,7,8
7 YBPR=EN*(1.+2.2*ENPR/EN**((2.00/3.00)+0.015*ENPR))
GO TO 11
8 YBPR = EN*(1.+1.3*ENPR/EN**(.5+.011*ENPR))
11 ENPR = 10.**ENPR
GAMPR = DGAM(YBPR,N=1)
PYB = .5**(.1./ENPR)
SUML = SUMLG(N=1)
IF(GAMPR=PYB) 10,12,12
10 H = .01
GO TO 14
12 H = -.01
14 Y0 = YBPR
E0 = DEVAL(Y0,N=1,SUML)
16 Y1 = Y0+H
E1 = DEVAL(Y1,N=1,SUML)
STEP = GAMPR + H*(E0+E1)/2.
IF ((DSTGN(1,00,STEP-PYB)=DSTGN(1,00,H)),EQ.0.) GO TO 20
18 Y0 = Y1
E0 = E1
GAMPR = STEP
GO TO 16
20 IF(H) 22,24,24
22 YB = Y1 - H*(PYB-STEP)/(GAMPR-STEP)
GO TO 30
24 YB = Y0 + H*(PYB-GAMPR)/(STEP-GAMPR)
30 BIAS = YB
777 YB = BIAS
NPREV = N
FAPREV = FA
X = SNR
K = KASE+1
GO TO (100,200,300,400,500), K

```

STATEMENT

```

100 SUM = 0.
P = EN*X
IF(YR=P+E) 150,102,102
102 KS = -(EN+1.)/2. + DSGRT(((EN+1.)/2.)**2+P*YB)
KS = MAX0 (KS,0)
GS = 1.-GAM(YB,KS+N=1,TN)
TS = EVAL(P,KS)*GS
G = GS
K = KS
TERM = TS
TL = TN
110 TEMP = SUM+TERM
IF(SUM=TEMP) 112,116,116
112 SUM = TEMP
IF(K) 115,116,114
114 TERM = TERM*FL9AT (K)*(G+TL)/(P*G)
G = G+TL
K = K+1
TL = TL+FL9AT (K+N)/YB
GS TS 110
116 TL = TN*YB/FL9AT (KS+N)
K = KS+1
G = GS+TL
TERM = TS*P*G/(GS*FL9AT (K))
120 TEMP = SUM+TERM
IF(SUM=TEMP) 122,190,190
122 SUM = TEMP
TL = TL+YB/FL9AT (K+N)
K = K+1
TERM = TERM*P*(G+TL)/(G*FL9AT (K))
G = G+TL
GS TS 120
150 KS = -1. - EN/2. + DSGRT(EN**2/4.+P*YB)
KS = MAX0 (KS,0)
GS = GAM(YB,KS+N=1,TN)
IF(GS) 174,174,155
155 TS = EVAL(P,KS)*GS
G = GS
TERM = TS
K = KS
TL = TN
160 TEMP = SUM+TERM
IF(SUM=TEMP) 162,166,166
162 SUM = TEMP
IF(K) 165,166,164
164 TERM = TERM*FL9AT (K)*(G+TL)/(P*G)
G = G+TL
TL = TL+FL9AT (K+N=1)/YB
K = K+1
GS TS 160
166 TL = TN*YB/FL9AT (KS+N)

```

STATEMENT

```

K = KS+1
G = GS-TL
TERM = TS*P*G/(GS*FL9AT (K))
170 TEMP = SUM + TERM
IF(SUM=TEMP) 172,174,174
172 SUM = TEMP
TL = TL*YB/FL9AT (K+N)
TERM = TERM*P*(G=TL)/(G*FL9AT (K+1))
G = G+TL
K = K+1
GO TO 170
174 SUM = 1.-SUM
190 PN = SUM
GO TO 90
200 IF(N=1) 210,210,220
210 PN = DEXP(-YB/(1.+X))
GO TO 90
220 TEMP = 1. + 1./(EN*X)
PN = 1. - GAM(YB,N=2,DUM) + DEXP((EN-1.)*ALOG(TEMP)-YB/(1.+EN*X))
* *GAM(YB/TEMP,N=2,DUM)
GO TO 90
300 IF(N=1) 310,310,320
310 PN = DEXP(-YB/(1.+X))
GO TO 90
320 PN = 1. - GAM(YB/(1.+X),N=1,DUM)
GO TO 90
400 IF(N=2) 410,420,430
410 PN = (1.+2.*X*YB/(X+2.)*2.)*DEXP(-2.*YB/(2.+X))
GO TO 90
420 PN = (1.+YB/(1.+X))*DEXP(-YB/(1.+X))
GO TO 90
430 C = 2. / (2.+EN*X)
D = 1.-C
IF(YB*D=EN) 440,450,450
440 SUM = 0.
TERM = 1.
J = N
442 TEMP = SUM+TERM
IF(SUM=TEMP) 444,446,446
444 SUM = TEMP
TERM = TERM*YB*D/FL9AT (J)
J = J+1
GO TO 442
446 PN = 1. - GAM(YB,N=2,DUM) + C*YB*EVAL(YB,N=2)
* * + D*EVAL(YB,N=1)*(1.+C*YB-(EN=2.)*C/D)*SUM
GO TO 90
450 PN = 1. - GAM(YB,N=3,DUM) + YB*EVAL(YB,N=3)*C/D
* * + DEXP(-C*YB-(EN=2.)*ALOG(D))*(1.+C*YB-(EN=2.)*C/D)
* * *GAM(YB*D,N=3,DUM)
GO TO 90
500 SUM = 0.

```

STATEMENT

```

C = 2. / (2.+X)
D = 1.-C
G = C/D
P = C+YB
KS = (3.*EN+(YB*D))/2. - DSGRT((EN=1.+(YB*D))**2/4.+(YB*D)*(EN+1.))
KS = MIN0 (KS,N)
KS = MAX0 (KS,N)
K = KS
J = N-KS
FKS = KS
K = MIN0 (KS,N)
IF(YB=EN*(1.+D)) 550,501,501
501 GS = 1. = GAM(P,2+N=1-KS,TN)
IF(GS) 526,526,502
502 TS = DEXP(FKS+ALOG(C)+(EN-FKS)*ALOG(D)+SUMLOG(N)-SUMLOG(KS)
*           -SUMLOG(J)+ALOG(GS))
G = GS
TERM = TS
TL = TN
510 TEMP = SUM+TERM
IF(SUM=TEMP) 512,516,516
512 SUM = TEMP
IF(K) 516,516,514
514 TL = TL+P/FL9AT (2*N=K)
TERM = TERM+FL9AT (K)*(G+TL)/(G*FL9AT (N=K+1)*G)
G = G+TL
K = K+1
GO TO 510
516 IF(KS=N) 518,526,526
518 TERM = TS+G*FL9AT (N=KS)*(GS-TN)/(FL9AT (KS+1)*GS)
G = GS-TN
TL = TN*FL9AT (2*N=1-KS)/P
K = KS+1
520 TEMP = SUM+TERM
IF(SUM=TEMP) 522,526,526
522 SUM = TEMP
IF(K=N) 524,526,526
524 TERM = TERM+G*FL9AT (N=K)*(G+TL)/(FL9AT (K+1)*G)
G = G+TL
TL = TL+FL9AT (2*N=1-K)/P
K = K+1
GO TO 520
526 PN = SUM
GO TO 90
550 GS = GAM(P,2+N=1-KS,TN)
IF(GS) 576,576,552
552 TS = DEXP(FKS+ALOG(C)+(EN-FKS)*ALOG(D)+SUMLOG(N)-SUMLOG(KS)
*           -SUMLOG(J)+ALOG(GS))
G = GS
TERM = TS
TL = TN

```

STATEMENT

```

560 TEMP = SUM+TERM
      IF(SUM=TEMP) 562,566,566
562 SUM = TEMP
      IF(K) 566,566,564
564 TL = TL+P/FL9AT (2*N-K)
      TERM = TERM+FL9AT (K)*(G+TL)/(G*FL9AT (N-K+1)*G)
      G = G+TL
      K = K+1
      GO TO 560
566 IF(KS=N) 568,576,576
568 TERM = TS+R*FL9AT (N-KS)*(GS+TN)/(FL9AT (KS+1)*GS)
      G = GS+TN
      TL = TN*FL9AT (2*N-1-KS)/P
      K = KS+1
570 TEMP = SUM+TERM
      IF(SUM=TEMP) 572,576,576
572 SUM = TEMP
      IF(K=N) 574,576,576
574 TERM = TERM+G*FL9AT (N-K)*(G+TL)/(FL9AT (K+1)*G)
      G = G+TL
      TL = TL+FL9AT (2*N-1-K)/P
      K = K+1
      GO TO 570
576 PN = 1.-SUM
      GO TO 90
90 IF(PN) 91,94,92
91 PN = 0.
      GO TO 94
92 IF(PN<1.) 94,94,93
93 PN = 1.
94 RETURN
99 WRITE (61,9) N,FA ,SNR,KASE
9 FORMAT (1H0 /50H UNREASONABLE CALL SEQUENCE TO MARCUM, ZERO RESULT
*          745 GIVEN //4H N = I8,5X,5HFA = E16.8,5X,5HSNR =
*          E16.8,5X,6HKASE = I8)
PN = 0.
BIAS = 0.
RETURN
END

```

STATEMENT

```
FUNCTION DGAM(B,N)
DOUBLE PRECISION SUM, TERM,TEMP,FJ,DGAM, DEVAL, B, SUML,SUMLG
SUM = 0.
K = B
IF(K=N) 130,200,200
100 J = N+1
SUML = SUMLOG(J)
TERM = DEVAL(B,J,SUML)
110 TEMP = SUM+TERM
IF(SUM=TEMP) 15,20,20
15 SUM = TEMP
J = J+1
FJ = J
TERM = TERM*B/FJ
GO TO 10
20 DGAM = SUM
RETURN
200 J = N
SUML = SUMLOG(J)
TERM = DEVAL(B,J,SUML)
30 TEMP = SUM+TERM
IF(SUM=TEMP) 35,40,40
35 SUM = TEMP
IF(J=1) 40,36,36
36 FJ = J
TERM = TERM*FJ/B
J = J+1
GO TO 30
40 DGAM = 1.-SUM
RETURN
END
```

STATEMENT

```
FUNCTION DEVAL (Y,N,SUML)
DOUBLE PRECISION XPN,EN,DEVAL, Y,SUML
XPN = -Y
IF(N) 20,20,10
10 EN = N
      XPN = XPN+EN*DLOG(Y)-SUML
20 DEVAL = DEXP(XPN)
      RETURN
      END
```

STATEMENT

```
FUNCTION GAM(B,N,TN)
SUM = 0.
K = B
IF(K=0) 100,200,200
100 J = N+1
TERM = EVAL(B,J)
TN = TERM*FLOAT(J)/B
10 TEMP = SUM+TERM
IF(SUM-TEMP) 15,20,20
15 SUM = TEMP
J = J+1
FJ = J
TERM = TERM*B/FJ
GO TO 10
20 GAM = SUM
RETURN
200 J = N
TERM = EVAL(B,J)
TN = TERM
30 TEMP = SUM+TERM
IF(SUM-TEMP) 35,40,40
35 SUM = TEMP
IF(J=1) 40,36,36
36 FJ = J
TERM = TERM*B/FJ
J = J+1
GO TO 30
40 GAM = 1.*SUM
RETURN
END
```

STATEMENT

```
FUNCTION EVAL(Y,N)
XPEN = -Y
IF(N) 20,29,10
10 EN = N
XPEN = XPEN+EN*ALOG(Y)-SUMLOG(N)
20 EVAL = EXP (XPEN)
RETURN
END
```

STATEMENT

```
FUNCTION SUMLOG(N)
DOUBLE PRECISION A, B, SUMLOG
DIMENSION A(1000)
DATA DUMA / 0. /
DATA DUMB / 0. /
DATA NLAST/1/
NMAX=1000
IF(DUMA=DUMB) 20,10,20
10 DUMA = 1.
DUMB = 0.
NLAST = 1
A(1) = 0.
20 NN = IABS (N)
IF(NN=1) 30,30,40
30 SUMLOG = 0.
RETURN
40 IF(NN>NLAST) 50,50,60
50 SUMLOG = A(NN)
RETURN
60 K = NLAST+1
IF(NN=NMAX) 70,70,80
70 DO 72 I=K,NN
72 A(I) = A(I-1) + DL2G(DFL2AT(I))
NLAST = NN
GO TO 50
80 IF(NLAST=NMAX) 82,90,90
82 DO 84 I=K,NMAX
84 A(I) = A(I-1) + DL2G(DFL2AT(I))
NLAST = NMAX
90 B = A(NMAX)
K = NMAX+1
90 92 I=K,NN
92 B = B + DL2G(DFL2AT(I))
SUMLOG = B
RETURN
END
```

STATEMENT

```

SUBROUTINE RHACHT(XMAX,YMAX,RMAX,HMAX,ANTHGT)
EXTERNAL F1
DIMENSION SN(181), RN1(181), TN1(181), JA(6)
DIMENSION XZ(180),YZ(180)
DIMENSION IRFAC(5), IHFAC(8)
COMMON /A/ REF, GRAD, RAD, CONST, U(182), N
COMMON /MTPE/ X22,Y22,X11,Y11,XAA,YAA,ERRRR
DIMENSION IANG(9),AANG(9)
COMMON /B/ XX(181), YY(181), CT1(181), SN1(181), DEL
DATA ERRRR / .001/
DATA REF/.000313/
DATA GRAD/.00004384822/
DATA IANG/1,26,31,51,71,121,151,172,181/
DATA AANG/0.,.5,.1,.3,.5,.10,.30,.50,.90./
DATA IHFAC/50,100,500,1000,5000,10000,50000,100000/
DATA IRFAC/5,10,50,100,500/
DATA JA/31,51,71,121,151,172/
CALL PENCHG(10)
DEL=XMAX*.01
IF (YMAX.LT.XMAX) DEL=YMAX*.01
BA = 6078.1155*RMAX*YMAX/(HMAX*XMAX)
BA2 = BA*BA
PREC = .00001
CONST = .3048/1852.0
RAD=20898950.13+ANTHGT
AB = 1.0 + REF
AB2 = AB*AB
CD = 2.0 * REF + REF*REF
ELEV = -.02
II=0
DO 29 JI=1,6
  G8 T0 (490,491,492,493,494,495), JI
490 ADEL = .02
  MM=26
  G8 T0 51
491 ADEL = .1
  MM=95
  G8 T0 51
492 ADEL=.5
  MM=20
  G8 T0 51
493 ADEL = 1.0
  MM=25
  G8 T0 51
494 ADEL=2.5
  MM=12
  G8 T0 51
495 ADEL=5.0
  MM=3
51 DO 29 IK = 1,MM
  II=II+1

```

STATEMENT

```

ELEV=ELEV+ADEF
RDN = ELEV/57.29577957
SN(I) = SIN(RDN)
S = SN(I)**2
U(I) = AB2*S=CD
IF (I.GE.181) GO TO 361
360 TN = TAN (RDN)
RDN1 = ATAN (BA*TN)
TN1(I) = TAN (RDN1)
CT1(I) = COS(RDN1)
SN1(I) = SIN(RDN1)
GO TO 29
361 CT1(I) = 0.0
SN1(I) = 1.0
29 CONTINUE
B=BA*XMAX
D 290 IX= 1,180
BAT=SQRT(BA2+(TN1(IX))**2)
YZ(IX)=XMAX*BA/BAT
290 YZ(IX)=B*TN1(IX)/BAT
H1 = 0.0
IJM = 100
JMAX = INT (ALCG10(HMAX) + .477122)
HINT=10.**(JMAX-1)
IJG = (HMAX/(10.**(JMAX-1))+ .001)
HMX=IJG*10**(JMAX-1)
D 30 J = 1, JMAX
IF (J .EQ. JMAX) IJM = IJG
IF (J.NE.1) GO TO 3
2 IJ = 10
GO TO 4
3 IJ = 20
4 D 30 I = IJ,IJM,10
H2 = I * 10 ** (J - 1)
IF(H2.EQ.HMX) CALL PENCHG(11)
D 304 K = 1, 181
N=182-K
IF (H2 .EQ. 10 .) RNG1(N) = 0.0
IF (H2.EQ.10..AND.N.EQ.1) GO TO 6
GO TO 7
6 GAM = REF*GHAD/AB
RI = 1.0/RAD
GG = 2.0*(RI - GAM)
RNG2 = (CONST*AB/GG)*2.0*SQRT(GG*H2)
GO TO 8
7 CALL SIMCON (H1,H2,PREC ,15,RINC,Nc1,P,F1)
RNG2 = RNG1(N) + RINC
8 RNG1(N) = RNG2
IF (H2 .LT. HINT) GO TO 304
A = RNG2*XMAX/RMAX
B = BA*A

```

STATEMENT

```

IF (N,NE,181) GO TO 47
46 CALL PL9T (0.,R,3)
XX(181) = 0.
YY(181) = R
X=0.
Y=R
X22=0.
Y22=R
GO TO 304
47 XLAST = X
YLAST = Y
XA=XZ(N)/XMAX
YA=YZ(N)/YMAX
48 IF (H2,NE,HMAX) GO TO 68
67 XX(N)=X
YY(N)=Y
68 IF(K,NE,2) GO TO 781
780 X11=X
Y11=Y
XAAXX
YAA = Y
GO TO 304
781 IF (X,LE,(XZ(N)+.0001)) GO TO 783
782 CALL INTST (XLAST,YLAST,X,Y,XZ(N),YZ(N),XZ(N+1),YZ(N+1),X0,Y0)
CALL MINTAP (X0,Y0)
CALL PL9T (X0,Y0,2)
IF (H2,EG,HMAX) GO TO 785
GO TO 305
783 IF (K,NE,181) GO TO 784
784 CALL MINTAP (X,Y)
CALL PL9T(X,Y,2)
XCOR = X
YCOR = Y
GO TO 304
785 CALL MINTAP (X,Y)
304 CONTINUE
305 H1 = H2
30 CONTINUE
GO TO 789
785 CALL PL9T(XZ(1),0.,3)
D9 786 NK=1,N
XX(NK)=XZ(NK)
YY(NK)=YZ(NK)
786 CALL PL9T(XX(NK),YY(NK),2)
CALL PL9T(X0,Y0,2)
XCOR = X0
YCOR = Y0
789 X=0.
Y = YMAX
CALL PL9T(X,Y,3)
Y = 0.0

```

STATEMENT

```

CALL PLAT(X,Y,2)
XA=X
CALL PLAT(X,Y,2)
CALL PENCHE(10)
KAMERMAX=1.
INTR=10
IF(RMAX.LT. 100.) INTR=5
IF(RMAX.GT. 300.) INTR=25
D 31 KAZINTR,KAM,INTR
RG = XA
A = RG*XMAX/RMAX
B = BA+A
D 38 KC = 1, 181
KR=KC
IF (KC.NE.181) GO TO 92
91 CALL MINTAP (0.,B)
CALL PLAT(0.,B,2)
GO TO 31
92 X=A*XZ(KC)/XMAX
IF (X.GT.XX(1)) GO TO 31
Y=A*YZ(KC)/XMAX
IF (Y.LE.(YY(KC)+.0001)) GO TO 72
73 IF (KR.NE.K+1) GO TO 731
730 X1=XCOR
Y1=YCOR
GO TO 732
731 X1=XX(KR-1)
Y1 = YY(KR-1)
732 X2=XX(KR)
Y2 = YY(KR)
XBX
YB = Y
CALL INTRST (X1,Y1,X2,Y2,XA,YA,XB,YB,X0,Y0)
CALL PLAT(X0,Y0,2)
GO TO 31
72 XA = X
YA = Y
IF (KC.NE.1) GO TO 86
85 CALL PLAT(X,Y,3)
X22=X
Y22=Y
GO TO 38
86 IF (KC.NE.2) GO TO 861
860 X11=X
Y11=Y
XA1=X
YA1=Y
GO TO 38
861 CALL MINTAP (X,Y)
38 CONTINUE
31 CONTINUE

```

STATEMENT

```

700 CALL ATICK(1,26,5,4,5)
CALL ATICK(27,71,1,5,10)
CALL ATICK(73,141,2,0,5)
CALL ATICK(142,151,1,0,5)
CALL ATICK(158,166,5,0,2)
CALL ATICK(168,178,2,1,2)
CALL ATICK(179,181,1,1,2)
DO 34 KF = 1, 6
NF = JA(KF)
X = 0.0
Y = 0.0
CALL PLST(X,Y,3)
X = XX(NF)
Y = YY(NF)
CALL PLST(X,Y,2)
34 CONTINUE
KT = 9
DO 364 KY = 1, 800
KT = KT + 1
IF (KT.NE.10) GO TO 369
368 FAC = 2.0
KT = 0
GO TO 370
369 FAC = 1.0
370 R2 = KY - 1
X = R2*XMAX/RMAX
IF (X .GT. (XMAX + .0001)) GO TO 365
Y = 0.0
CALL PLST(X,Y,3)
Y = - FAC * DEL
CALL PLST(X,Y,2)
364 CONTINUE
365 KS = 9
KJM = HMAX / HINT + 1.001
DO 37 KJ = 1, KJM
KS = KS + 1
IF (KS.NE.10) GO TO 376
375 FAC = 2.0
KS = 0
GO TO 377
376 FAC = 1.0
377 H = HINT * (KJ -1)
Y = H*YMAX/HMAX
X = 0.0
CALL PLST(X,Y,3)
X = - FAC * DEL
CALL PLST(X,Y,2)
37 CONTINUE
CALL PENCHG(11)
IF (XMAX=Y"AX) 460,460,461
460 SFAC=XMAX *.125

```

STATEMENT

```
G9 TO 452
451 SFAC=SYMAX*.125
452 H=.175*SFAC
    DO 100 IH = 1, 5
    NR = R'AX / IRFAC (IR)
    IF (NR.GT.10) G9 TO 100
101 IRUNIT = IRFAC (IR)
    G9 TO 102
102 CONTINUE
    IRUNIT=IRFAC(5)
102 DO 110 IH = 1, 8
    NH = HMAX / IHFAC (IH)
    IF (NH.GT.10) G9 TO 110
103 IHUNIT = IHFAC (IH)
    G9 TO 128
110 CONTINUE
    IHUNIT=IHFAC(8)
128 X=-.05*SFAC
    Y=-.5*SFAC
    CALL INUMFR (X,Y,H,0,0.0)
    N = IRUNIT
129 IDGITS=ALOG10(FLSAT(N))+1.000001
    CALL SENTER (H, IDGITS, IDGITS, BIAS)
    X = (N/RMAX) * XMAX - BIAS
    IF (X + BIAS .GT. XMAX) G9 TO 801
    CALL INUMBP (X,Y,H,N,0.0)
    N = N + IRUNIT
    G9 TO 120
801 Y=-1.0*SFAC
    CALL SENTER (H, 21,21,BIAS)
    X = 0.5 * XMAX - BIAS
    CALL LFTTER (X,Y,H,21H RANGE, NAUTICAL MILES,0.0,21)
    X=-.5*SFAC
    Y=-.0875*SFAC
    CALL INUMFR (X,Y,H,0,0.0)
    N = IHUNIT
121 IHGITS=ALNG10(FLSAT(N))+3.000001
    X=-0.15*IHGITS*SFAC
    Y=(N/HMAX)*YMAX-.0875*SFAC
    IF (Y .GT. YMAX) G9 TO 803
    CALL INUMBP (X,Y,H,N,0.0)
    N = N + IHUNIT
    G9 TO 121
803 X = -1.40*SFAC
    CALL SENTER(H,33,33,RIAS)
    Y = 0.5 * YMAX - BIAS
    CALL LFTTER (X,Y,H,33HTARGET HEIGHT ABOVE ANTENNA, FEET,90.,33)
    X1=X-3.*H
    CALL SENTER(H,26,26,RIAS)
    CALL LFTTER (X1,Y,H,26H(ANTENNA HEIGHT=      FEET),90.,26)
    Y2=Y+10.5714*H
```

STATEMENT

```
CALL NUMBER (X1,Y2,H,ANTHGT,90.,-1)
XPRZ=2.*XMAX
YPRZ=2.*H
804 IL = 1, 9
IND = IANG(IL)
AAN=AANG(IL)
CX=.1
IF (IL.GE.6)CX=.125
X=XX(IND) + .4*CT1(IND)*SFAC = CX*SFAC
Y=YY(IND) + .4*SN1(IND)*SFAC = .0875*SFAC
IF (IL.EQ.9) X = X + H
IF (IL.EQ.9,OR.(Y=YPR).GT.(1.5*H)) GO TO 880
IF ((XPR-X).LT.(4.0*H),OR.X.LT.2.*H) GO TO 804
880 XPR=X
YPR=Y
IF (IL.GE.6) GO TO 888
887 CALL NUMBER (X,Y,H,AAN,0,0,-1)
X = X + .15 * SFAC
GO TO 889
888 CALL NUMBER (X,Y,H,AAN,0,0,-1)
889 CONTINUE
CALL DEGREE (X + .35*SFAC, Y + .175 * SFAC,.08*SFAC)
804 CONTINUE
END
```

STATEMENT

```
FUNCTION F1(X)
COMMON /A/ REF, GRAD, RAD, CRNST, U(162), N
N=REF*EXP(-GRAD*X)
CC=X/RAD
V=2.0*BB+BB*FB
X=2.0*CC+CC*FC
FX = SQRT (U(N) + V + W + V*X)
F1 = CRNST * (1.0 +V)*(1.0 + CC)/FX
END
```

STATEMENT

```
SUBROUTINE SIMCRN(X1,XEND,TEST,LIM,AREA,NCI,R,F)
NCI=0
ODD=0.0
INT#1
V=1.0
EVEN=0.0
AREA1=0.0
19 ENDS=F(X1)+F(XEND)
2 H=(XEND-X1)/V
3 ODD=EVEN+ODD
4 X=X1+H/2.
5 EVEN=0.0
6 DO 3 I=1,INT
7     EVEN=EVEN+F(X)
8     X=X+H
9 CONTINUE
10 AREA=(ENDS+4.0*EVEN+2.0*ODD)*H/6.0
11 NCI=NCI+1
12 R=ABS ((AREA1-AREA)/AREA)
13 IF(NCI=LIM)341,35,35
141 IF(R=TEST)35,35,4
15 RETURN
16 AREA1=AREA
17 INT#2*INT
18 V#2.0#V
19 GO TO 2
20 END
```

STATEMENT

```
ROUTINE ATICK (IA,JA,KA,MR,MC)
CRHMH /F/ XX(1E1), YY(1E1), CT1(1E1), SN1(1E1), DEL
MA = MR
DO 1 K = IA,JA,KA
MA = MA + 1
IF (MA,NE,MC) GO TO 3
2 FAC = 2.0
MA = n
GO TO 4
3 FAC = 1.0
4 X = XX(K)
Y = YY(K)
CALL PLST(X,Y,3)
X = X + DEL*FAC*CT1(K)
Y = Y + DEL*FAC*SN1(K)
CALL PLST(X,Y,2)
1 CONTINUE
END
```

STATEMENT

```
SUBROUTINE SENTER (H,N,I,BIAS)
CONST = .2857143 * H
WIDTHF = (3*I-1) * CONST
WIDTHN = (3*N-1) * CONST
BIAS = WIDTHF + 0.5 * WIDTHN
RETURN
END
```

STATEMENT

```
SUBROUTINE MINTAP (X,Y)
COMMON /MTPR/ X2, Y2, X1, Y1, XA, YA, ERRPR
COMMON /MN/ M,N
DATA M/0/
DATA N/0/
DX(U1,V1,U2,V2) = SQRT((U2-U1)**2 + (V2-V1)**2)
D1 = DX(X1,Y1,X2,Y2)
IF (D1 .EQ. 0.) GO TO 11
U2 = DX(X,Y,X1,Y1)
IF (D2 .EQ. 0.) GO TO 2
D3 = DX(X,Y,X2,Y2)
D11 = DX(XA,YA,X2,Y2)
IF (D3 .LT. D11) GO TO 1
COSN = (D3*D3-D2*D2-D1*D1)/(2.*D1*D2)
IF (COSN .GT. 1. .OR. COSN .LT. -1.) COSN = 1.
SINE = SQRT(1. - COSN*COSN)
DEVN = D2*SINE
IF (DEVN .LE. ERRPR) GO TO 2
1 CALL PLST (XA,YA,2)
M = M+1
X2 = XA
Y2 = YA
11 X1 = X
Y1 = Y
2 XA = X
YA = Y
N = N+1
END
```

STATEMENT

```
SUBROUTINE SEAREF (FMHZ, PSI, IPOL, RHO, PHI)
  COMPLEX EPSC, GAM, SQTERM, TERM
  DATA FLAST / 0. /
  SINPSI = SIN (PSI)
  CSPSI = COS(PSI)**2
  IF (FMHZ .EQ. FLAST) GO TO 200
  FLAST = FMHZ
  * = 299.793 / FMHZ
  IF (FMHZ .GT. 1500.) GO TO 151
150 SIG = 4.3
  EPS1 = 80.
  GO TO 155
151 SIG = 4.3 + (FMHZ - 1500.) * .00148
  IF (FMHZ .GT. 3000.) GO TO 154
153 EPS1 = 80. - (FMHZ - 1500.) * .00733
  GO TO 155
154 EPS1 = 69. - (FMHZ - 3000.) * .002429
  SIG = 6.52 + (FMHZ - 3000.) * .001314
155 EPSC = CMPLX (EPS1,-60.*W*SIG)
200 SQTERM= CSQRT(EPSC-CSPSI)
  IF (IPOL .NE. 1 ) GO TO 161
160 TERM = EPSC * SINPSI
  GAM = (TERM-SQTERM)/(TERM+SQTERM)
  GO TO 180
161 GAM = (SINPSI - SQTERM) / (SINPSI + SQTERM)
180 RHO = CABS (GAM)
  PHI = ATAN2 (AIMAG(GAM), REAL (GAM))
  RETURN
END
```

STATEMENT

```
SUBROUTINE DEGREE(X,Y,H)
DIMENSION DELX(8), DELY(8)
DATA DELX/-0.7071,-1.0,-0.7071,0.0,0.7071,1.0,0.7071,0.0/
DATA DELY/0.7071,0.0,-0.7071,-1.0,-0.7071,0.0,0.7071,1.0/
D = H*.414214
X = X + .5*H
Y = Y + .5*D
CALL PLOT (X,Y,3)
DO 1 II = 1, 8
  X = X + DELX(II)*D
  Y = Y + DELY(II)*D
1 CALL PLOT(X,Y,2)
END
```

STATEMENT

```

SUBROUTINE INTSECT (X1,Y1,X2,Y2,XA,YA,XB,YB,X0,Y0)
IF (ABS(X2-X1),GE,10,E=76) GO TO 2
1 IF (ABS(Xe-XA),LT,10,E=76) GO TO 99
X0 = X1
S = (YB-YA)/(XB-XA)
Y0 = S*(X0-XA) + YA
RETURN
2 IF (ABS(XB-XA),GE,10,E=76) GO TO 4
3 IF (ABS(X2-X1),LT,10,E=76) GO TO 99
X0 = XA
S = (Y2-Y1)/(X2-X1)
Y0 = S*(X0-X1) + Y1
RETURN
4 S1 = (YB-YA)/(XB-XA)
S2 = (Y2-Y1)/(X2-X1)
IF (S1 ,EQ, 0.) GO TO 5
IF (ABS(S2-S1),LT,10,E=76) GO TO 99
RT0 = S2/S1
Y0 = (Y2+S2*(XA-X2)-YA*RT0)/(1.-RT0)
X0 = (Y0-YA)/S1 + XA
RETURN
5 IF (S2 ,EQ, 0.) GO TO 99
X0 = (YA-Y2)/S2 + X2
Y0=YA
RETURN
99 PRINT 100, X1, Y1
PRINT 101, X2,Y2,XA,YA,XB,YB
X0 = 0.
Y0 = 0.
100 FORMAT (3X,6HCALL TO INTSECT ABORTED. LINES PARALLEL, NO INTERSE
*CTION. X1 = ,E10.2,6H Y1 = ,E10.2)
101 FORMAT(3X, 6H X2 = ,E10.2,6H Y2 = ,E10.2,
* 6H YA = ,E10.2,6H YA = ,E10.2,6H XB = ,E10.2,6H YB = ,E10.2 //)
END

```

STATEMENT

```
SUBROUTINE ARRAA (X1,Y1,X2,Y2,TIPL)
COMMON/AG/ANG
DATA ANG / .35/
YA = Y2 - Y1
XA = X2 - X1
A = ATAN2(YA,XA)
A3 = A + ANG
A4 = A - ANG
X3 = X2 - TIPL * COS(A3)
Y3 = Y2 - TIPL * SIN(A3)
X4 = X2 - TIPL * COS(A4)
Y4 = Y2 - TIPL * SIN(A4)
CALL PLST (X1, Y1, 3)
CALL PL9T (X2, Y2, 2)
CALL PL9T (X3, Y3, 2)
CALL PL9T (X4, Y4, 3)
CALL PL9T (X2, Y2, 2)
END
```

STATEMENT

```
SUBROUTINE REZERO
ENTRY  PE1CHG
ENTRY  DASHON
ENTRY  DASHOF
END
```

APPENDIX B: Input Data Card Formats for LOBMUF (For ASC - Jan 1977)

Program LOBMUF will plot the envelope of N radars using the pattern calculations contained in the original program described in NRL Report 7098 by L. Blake. Incoherent integration is assumed. An antenna height must be specified in subroutine RHACHT. The parameter name for this antenna height is ANTHITE and is used to draw the range-height grid. The actual antenna heights for the individual radars are input separately and used for the multipath calculations. ANTHITE is not very important except for the labeling of the height axis of the grid.

Input Card Sequence

Col.

1. ANTHITE in F10.0 field	
2. Label Card	
3. Grid Parameters in F10.0 fields:	
a. XMAX	1-10
b. YMAX	11-20
c. RMAX	21-30
d. HMAX	31-40
e. THMIN	41-50
f. THMAX	51-60
g. WHFT	61-70
h. RDR	71-80

XMAX = maximum X-dimension of chart in inches

YMAX = maximum Y-dimension of chart in inches

RMAX = maximum range of chart in nautical miles

HMAX = maximum height on chart in feet

THMIN = minimum elevation angle for the plot

THMAX = maximum elevation angle for the plot

WHFT = sea wave height in feet

RDR = number of radars for which an envelope is to be plotted.

4. Common Parameters in F10.0 fields:

a. PDT	1-10
b. PFA	11-20
c. PULS (total number of pulses)	21-30
d. CASE	31-40
e. AHFT	41-50
f. TILT	51-60
g. POL	61-70
h. CSC	71-80

PDT = probability of detection

PFA = false alarm exponent, i.e., the positive value of the exponent (power of ten); for 10^{-6} , enter the number 6.0, etc.

PULS = total number of pulses

CASE = Swerling case number
AHFT = antenna height in feet
TILT = tilt angle of the antenna beam maximum with respect to the horizon in degrees.

For reference, POL is polarization as follows:

POL = 1. vertical
POL = 2. horizontal

CSC is for pencil or cosecant squared antenna pattern:

CSC = 0. pencil beam
CSC = 1. cosecant squared beam

5. Radar Parameters in F10.0 fields:

a. RFS	1-10
b. FMHZ	11-20
c. BWD	21-30
d. SLDB	31-40
e. PULNUM (number pulses at FMHZ)	41-50
f. FREF	51-60

Repeat card 5 for N repetitions.

RFS = calculated or assumed free-space range of the radar on the specified target

FMHZ = radar frequency in megahertz

BWD = antenna half-power beamwidth in degrees

SLDB = first elevation sidelobe level relative to the main lobe

PULNUM = number of pulses at each specified frequency

FREF = frequency used to calculate RFS if RFS was calculated for the total number of pulses (PULS)

FREF = 0, if RFS was calculated at each frequency using PULNUM.

After cards 1-5, the sequence can be repeated as many times as desired, starting with card 2.

A note of caution is that the elevation plot angle increment is determined by

$$\frac{\text{THMAX} - \text{THMIN}}{2000}$$

The value has proven adequate for S-band radars where 10° and 0° were the values for THMAX and THMIN. It is recommended that an envelope for a single radar (RDR = 1) be run when there is doubt that this angle increment is small enough.